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Extremal problems and generalized degrees. (In English)

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Authors' abstract: For a positive integer n and a graphical property P, $\operatorname{ext}_n(P)$ will denote the minimum number of edges in a graph G of order n that satisfies property P, and $\operatorname{Ext}_n(P)$ will denote the class of graphs with n vertices and $\operatorname{ext}_n(P)$ edges that have property P. The extremal numbers $\operatorname{ext}_n(P)$ for properties P that have been commonly used as sufficient conditions for Hamiltonian paths and cycles in graphs will be investigated. In particular, results on the extremal numbers for generalized degree and generalized independent degree properties will be given, where for a fixed positive integer t, the generalized degree $\delta_t(G)$ (generalized independent degree $\delta_t^i(G)$) is the minimum number of vertices in the union of the neighborhoods of a set of t (independent) vertices of the graph G.

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