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Sure monochromatic subset sums. (In English)

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Let  $f(n)$  denote the smallest integer  $f$  such that one can color the integers  $\{1, 2, \dots, n-1\}$  by  $f$  colors so that there is no monochromatic subset the sum of whose elements is  $n$ . It is shown that

$$\Omega\left(\frac{n^{1/3}}{\log^{4/3} n}\right) \leq f(n) \leq O\left(\frac{n^{1/3}(\log \log n)^{1/3}}{\log^{1/3} n}\right).$$

The lower bound settles a problem of Erdős.

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