

THE DISTANCE MATRIX OF A BIDIRECTED TREE*

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Abstract. A bidirected tree is a tree in which each edge is replaced by two arcs in either direction. Formulas are obtained for the determinant and the inverse of a bidirected tree, generalizing well-known formulas in the literature.

Key words. Tree, Distance matrix, Laplacian matrix, Determinant, Block matrix.

AMS subject classifications. 05C50, 15A15.

* Received by the editors May 18, 2008. Accepted for publication April 10, 2009. Handling Editor: Bryan L. Shader.

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