

COMPLETING BLOCK HERMITIAN MATRICES WITH MAXIMAL AND MINIMAL RANKS AND INERTIAS*

YONGGE TIAN[†]

Abstract. For a Hermitian matrix with its main block diagonal given, this paper shows how to choose the off-diagonal blocks such that the resulting matrix has the maximal and minimal possible ranks and inertias, respectively. Some direct consequences and applications are also given.

Key words. Hermitian matrix, partial matrix, rank, inertia, matrix completion, matrix decomposition.

AMS subject classifications. 15A03, 15A23, 15A57.

*Received by the editors on June 15, 2009. Accepted for publication on July 31, 2010. Handling Editors: Roger A. Horn and Fuzhen Zhang.

[†]China Economics and Management Academy, Central University of Finance and Economics, Beijing 100081, China (yongge.tian@gmail.com).