

DERIVATIVES OF THE DIAMETER AND THE AREA OF A CONNECTED COMPONENT OF THE PSEUDOSPECTRUM*

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Abstract. The paper concerns the relation between the following two quantities.

- (i) The Hölder condition number of an eigenvalue λ of a square complex matrix.
- (ii) The rate of growth of the diameter and the area of the connected component of the ε -pseusospectrum containing λ .

Key words. Matrices, Pseudospectra, Condition number, Eigenvalues, Derivatives.

AMS subject classifications. 15A12, 15A18, 15A60, 65F35.

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