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## THE NUMERICAL RANGE OF LINEAR OPERATORS ON THE 2-DIMENTIONAL KREIN SPACE\*

HIROSHI NAKAZATO<sup>†</sup>, NATÁLIA BEBIANO<sup>‡</sup>, AND JOÃO DA PROVIDÊNCIA§

Abstract. The aim of this note is to provide the complete characterization of the numerical range of linear operators on the 2-dimensional Krein space  $\mathbb{C}^2$ .

 ${\bf Key}$  words. Krein space, Numerical range, Rank one operator.

AMS subject classifications. 46C20, 47A12.

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<sup>&</sup>lt;sup>†</sup>Department of Mathematical Sciences, Hirosaki University, 036-8561, Japan (nakahr@cc.hirosaki-u.ac.jp).

<sup>&</sup>lt;sup>‡</sup>Mathematics Department, University of Coimbra, P3001-454 Coimbra, Portgal (bebiano@mat.uc.pt).

<sup>&</sup>lt;sup>§</sup>Physics Department, University of Coimbra, P3004-516 Coimbra, Portgal (providencia@teor.fis.uc.pt).