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SOME NEW LOWER BOUNDS FOR THE MINIMUM EIGENVALUE OF THE HADAMARD PRODUCT OF AN *M*-MATRIX AND ITS INVERSE*

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Abstract. For the Hadamard product $A \circ A^{-1}$ of an *M*-matrix *A* and its inverse A^{-1} , some new lower bounds for the minimum eigenvalue of $A \circ A^{-1}$ are given. These bounds improve the results of [H.B. Li, T.Z. Huang, S.Q. Shen, and H. Li. Lower bounds for the minimum eigenvalue of Hadamard product of an *M*-matrix and its inverse. *Linear Algebra Appl.*, 420:235-247, 2007] and [Y.T. Li, F.B. Chen, and D.F. Wang. New lower bounds on eigenvalue of the Hadamard product of an *M*-matrix and its inverse. *Linear Algebra Appl.*, 430:1423-1431, 2009].

Key words. Hadamard product, M-matrix, Inverse, Minimum eigenvalue, Lower bounds.

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