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## RECURSIVE COMPUTATION OF CERTAIN INTEGRALS OF ELLIPTIC TYPE*

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Abstract. An algorithm for the numerical calculation of the integral function

$$
N_{n}(x)=\int_{0}^{\pi / 2} \frac{\cos ^{2 n}(\Phi)}{\sqrt{1-x \cdot \sin ^{2}(\Phi)}} \cdot d \Phi \quad(0 \leq x<1 ; n=0,1,2, \ldots),
$$

distinguished solution of the second-order difference equation
$(2 n+1) \cdot x \cdot N_{n+1}(x)+2 n \cdot(1-2 x) \cdot N_{n}(x)=(2 n-1) \cdot(1-x) \cdot N_{n-1}(x) \quad(n=1,2, \ldots)$, that uses the recurrence relation and its related continued fraction expansion, is described and discussed. The numerical efficiency of the algorithm is analysed for various x values of the interval $(0 \leq x<1)$. A twelve digits tabulation of $N_{n}(x)$ for $n=1(1) 20$ and $x=0(0.02) 1$ is presented as example of the algorithm utilization.

Key words. recurrence relations, elliptic integrals, continued fractions
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