# ON GRADED QR DECOMPOSITIONS OF PRODUCTS OF MATRICES * 

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#### Abstract

This paper is concerned with the singular values and vectors of a product $M_{m}=$ $A_{1} A_{2} \cdots A_{m}$ of matrices of order $n$. The chief difficulty with computing them directly from $M_{m}$ is that with increasing $m$ the ratio of the small to the large singular values of $M_{m}$ may fall below the rounding unit, so that the former are computed inaccurately. The solution proposed here is to compute recursively the factorization $M_{m}=Q R P^{\mathrm{T}}$, where $Q$ is orthogonal, $R$ is a graded upper triangular, and $P^{\mathrm{T}}$ is a permutation.


Key words. QR decomposition, singular value decomposition, graded matrix, matrix product.

AMS subject classification. 65F30.

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