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QUADRATURE FORMULAS FOR RATIONAL FUNCTIONS*

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Abstract. Let ω be an L₁-integrable function on [-1, 1] and let us denote

$$I_{\omega}(f) = \int_{-1}^{1} f(x)\omega(x)dx,$$

where f is any bounded integrable function with respect to the weight function ω . We consider rational interpolatory quadrature formulas (RIQFs) where all the poles are preassigned and the interpolation is carried out along a table of points contained in $\overline{\mathbb{C}} \setminus [-1, 1]$. The main purpose of this paper is the study of the convergence of the RIQFs to $I_{\omega}(f)$.

Key words. weight functions, interpolatory quadrature formulas, orthogonal polynomials, multipoint Padé-type approximants.

AMS subject classifications. 41A21, 42C05, 30E10.

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