Geometry and Symmetry in Physics

## ON THE UNCERTAINTY RELATIONS IN STOCHASTIC MECHANICS

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## Abstract.

It is shown that the Bohm equations for the phase S and squared modulus  $\rho$  of the quantum mechanical wave function can be derived from the classical ensemble equations admiting an aditional momentum  $p_s$  of the form proportional to the osmotic velocity in the Nelson stochastic mechanics and using the variational principle with appropriate change of variables. The possibility to treat grad S and  $P_s$  as two parts of the momentum of quantum ensemble particles is considered from the view point of uncertainty relations of Robertson - Schrödinger type on the examples of the stochastic image of quantum mechanical canonical coherent and squeezed states.

## 1. Introduction

The uncertainty (indeterminacy) principle in quantum physics, which quantitatively is expressed in the form of uncertainty relations (URs) [13, 14, 24, 25] is commonly regarded as the most radical departure from the classical physics.

However in the recent decades publications have appeared [5, 11, 12, 21, 23] in which inequalities are introduced in Nelson stochastic mechanics (SM) [19] and discussed as Heisenberg-type URs. The equations of motion in this mechanics coincide with the David Bohm equations [1] (the continuity equation and the modified Hamilton-Jacobi equation, the latter known also as Hamilton-Jacobi-Madelung (HJM) equation) for the phase S and squared modulus  $|\psi|^2 \equiv \rho$  of the Schrödinger wave function  $\psi$ . Bohm equations for S and  $\rho$  have been later derived from 'the stochastic variational principles of control theory' by Guerra and Marra [9], and by Reginatto [23], using the 'principle of minimum Fisher information' [6].