

COMMON FIXED POINT THEOREM FOR OCCASIONALLY WEAKLY COMPATIBLE MAPPINGS IN MENGER SPACE

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Abstract. The concept of occasionally weakly compatible (shortly, owc) mappings introduced by Al-Thagafi and Shahzad [2], which is more general than the concept of weakly compatible maps. In this paper, we prove a common fixed point theorem for owc mappings in Menger space using arbitrary continuous t-norm for a nonlinear case.

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