

EXISTENCE AND ASYMPTOTIC BEHAVIOR OF SOLUTION TO A SINGULAR ELLIPTIC PROBLEM

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Abstract. In this paper we obtain existence results for the positive solution of a singular elliptic boundary value problem. To prove the main results we use comparison arguments and the method of sub-super solutions combined with a procedure which truncates the singularity.

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