

# PREFACE

This volume of RIMS Kôkyûroku Bessatsu is the proceedings of the RIMS Conference

## **“Expansion of Integrable Systems”**

held at Research Institute for Mathematical Sciences (RIMS), Kyoto University from August 11 through August 13, 2008.

In the conference, 14 invited speakers talked about their recent research on integrable systems and related topics. We hope it was a good opportunity for 74 participants to overview recent trends in integrable systems and get a hint for future research.

This volume collects 12 contributions from the speakers of the conference. All the papers are refereed. We thank the authors and anonymous referees for their great effort. Without their help this volume would not have been published.

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Atsushi NOBE

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