

**Corrigendum on Z.-Q. Chen, P. Kim, and
T. Kumagai: Global heat kernel estimates
for symmetric jump processes. *Trans.
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In the statement of Theorem 1.2(2.b) and Theorem 1.4 of [2], the following corrections should be made for the large time estimates:

- (i) page 5025, Eq (1.17) : $|\log \frac{|x-y|}{t}|$ should be $(1 + \log^+ \frac{|x-y|}{t})$ (two places).
- (ii) page 5027, Eq (1.21) : $\log \frac{|x-y|}{t}$ should be $(1 + \log^+ \frac{|x-y|}{t})$ (two places).

Similarly,

- (iii) page 5039, line 13 and page 5040, line 6: $(|x - y| \log(|x - y|/t) \wedge |x - y|^2/t)$ should be $(|x - y|(1 + \log^+ \frac{|x-y|}{t})) \wedge (|x - y|^2/t)$.
- (iv) page 5039, line -4: $(|x - y|(\log \frac{|x-y|}{t})^{(\beta_0-1)/\beta_0} \wedge |x - y|^2/t)$ should be $(|x - y|(1 + \log^+ \frac{|x-y|}{t})^{(\beta_0-1)/\beta_0}) \wedge (|x - y|^2/t)$.

This is because in the proof of [2, Theorems 1.2(2.b)], the case of $|x - y| \asymp t$ when $\beta \in (1, \infty)$ was missed to be considered. Once taking into account of this missing case, one can easily conclude from [2] that $1 + \log^+ \frac{|x-y|}{t}$ is the correct term. See [1, Proposition 6.7] for a proof of the lower bound estimate on the Dirichlet heat kernel in upper half space, which has this corrected term .

We take this opportunity to correct some typos in the paper and update a reference.

1. page 5022, line -5: “and” should be “which in particular implies that”
2. page 5024, Eq (1.15) and page 5026, Eq (1.19): the second C^{-1} should be C .
3. page 5028, line 4: Delete the last dw .
4. page 5028, line 12: Delete the last dz .
5. page 5029, line 1: β_3 should be β_* , say. (β_3 is used in (3.10).)
6. page 5031, Eq (3.7): $\|f\|_2$ should be $\|f\|_2^2$
7. page 5033, line -12: “ $|\xi - \eta| \leq t/C_*$ ” should be “ $|x - y| \leq t/C_*$ ”.
8. page 5035, line -2: “ $\lambda > 0$ ” should be “ $\lambda \geq b$ ”.
9. page 5036–5039, proof of Theorem 3.4: All β_3 in the proof of Theorem 3.4 should be β_1 except two β_3 ’s in (3.34) and one β_3 in the denominator of second term in page 5039 line 5, which comes from the upper bound of J_λ .
10. page 5037, line 1: “where the lower bound of (3.10)” should be “where the upper bound of (3.10)”.
11. Page 5037, line 8: β_8 should be β_1 .
12. Page 5037, line -13, -14: Change “Let $b := \frac{a\beta_3}{8(d+\beta_3)C^*}$ and note that $\phi_1^{-1}(t) \leq c_1\phi_2^{-1}(t)$ for $t \leq 1$ due to (3.12). By (3.10) and (3.25),” to “Let $b := \frac{a\beta_3}{8(d+\beta_3)C^*}$. By (3.25),”
13. Page 5039, line 1: (3.34) should be (3.36).
14. page 5040, line -2: c_2 should be c_1 .
15. page 5041, line -12: “ $(\mathcal{E}, \mathcal{F}) \dots$ ” should be “ $(\mathcal{Q}, \mathcal{D}) \dots$ ”.
16. page 5042, Eq (4.3): $q^\delta(t, x, y) \leq c_\delta t^{-d/2}$ should be $q^\delta(t, x, y) \leq c_\delta(\phi_2^{-1}(t)^{-d} \vee t^{-d/2})$
17. page 5042, Eq (4.4): $e^{-s\|\mathcal{J}_\delta\|_\infty}$ should be $e^{-t\|\mathcal{J}_\delta\|_\infty}$.
18. page 5042, line -11: $|x|$ and $|y|$ should be $|x - x_0|$ and $|y - x_0|$, respectively.
19. page 5042, Eq (4.5): $|x|$ should be $|x - x_0|$.

20. page 5042, line -4: $q^{\delta, B(x_0, r)}(t, x, y_0)$ should be $q^{\delta, B(x_0, r)}(t, \cdot, y_0)$.
21. page 5043, Theorem 4.6: Delete “for every $x_0 \in \mathbb{R}^d$ ” from the 2nd line of Theorem 4.6.
22. page 5043, line -15: $\varphi_r(\cdot)$ should be $\Phi_r(\cdot)$.
23. page 5043, Eq (4.8): $L^2(u, u)$ should be $L^2(\mathbb{R}^d; dx)$.
24. page 5044, line 13: $r^{d+2}J(rx, ry)$ should be $t r^{d+2}\widehat{J}_\delta(rx, ry)$.
25. page 5044, line -10: $(\log |w|/(r^2t))^{(\beta_0-1)/\beta_0}$ should be $(1+\log |w|/(r^2t))^{(\beta_0-1)/\beta_0}$
26. page 5044, Eq (4.12): Change $|w|_0^\beta$ to $|w|^{\beta_0}$.
27. page 5044, Eq (4.13): The first $1/4$ should be $1/2$.
28. page 5045, line 3–4: Change

$$G'(t) = - \int_B \int_B \dots dx dy - \int_B \dots dx$$

to

$$G'(t) = -c_5^{-1} \int_B \int_B \dots dx dy - c_5^{-1} \int_B \dots dx.$$

29. page 5045, line 13 and page 5045, line -9: $J^{(r)}(x, y)$ should be $\widehat{J}^{(r)}(x, y)$.
30. page 5045, line -14: β_2 should be β_3 .
31. page 5048, Eq (4.19): “ $z \in B_{3aR/2}$.” should be “ $z \in B_{3aR/2} \setminus B_{5aR/4}$.”
32. page 5049, line -4: “ $e^{-c_2|z-x|(\log |z-x|/t)^{(\beta-1)/\beta}}$ ” should be “ $t^{-d/2}e^{-c_2|z-x|(1+\log^+(|z-x|/t))^{(\beta-1)/\beta}}$ ”.
33. page 5050, line 3: “ $t e^{-c_8|z-x|^\beta}$ ” should be “ $t^{-d/2}e^{-c_8|z-x|^\beta}$ ”.
34. page 5050, Eq (5.2): $B(x, r)$ should be $B(x, r/4)$
35. page 5050, line 12: $\mathbb{P}_x(\tau_{B(x, 2r)} < \gamma r^2) = \mathbb{P}_x\left(\sup_{u \leq \gamma r^2} |Y_u - Y_0| > r\right)$
should be $\mathbb{P}_x(\tau_{B(x, r/2)} < \gamma r^2) = \mathbb{P}_x\left(\sup_{u \leq \gamma r^2} |Y_u - Y_0| > r/2\right)$.

36. page 5050, line 13: $t = 4\gamma r^2$ should be $t = \gamma r^2$.
37. page 5051, line -2: $|x - y|$ should be $|x - y|^\beta$.
38. page 5055, Reference [20]: Ann. Inst. H. Poincaré Probab. Statist. **47(3)** (2011), 650–662.

References

- [1] Z.-Q. Chen, P. Kim, Global Dirichlet Heat Kernel Estimates for Symmetric Lévy Processes in Half-space, arXiv:1504.04673.
- [2] Z.-Q. Chen, P. Kim, and T. Kumagai. Global heat kernel estimates for symmetric jump processes. *Trans. Amer. Math. Soc.*, 363(9):5021–5055, 2011.

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