# 数理解析研究所講究録1234

# Tosio Kato's Method and Principle for Evolution Equations in Mathematical Physics

京都大学数理解析研究所 2001年10月

#### **Preface**

The papers in this volume were written by the speakers at the international workshop "Tosio Kato's Method and Principle for Evolution Equations in Mathematical Physics", which was held at Hokkaido University on 27, 28, and 29 June, 2001.

Professor Tosio Kato, a professor emeritus of Mathematics at University of California, Berkeley, was a leading mathematician in the theory of evolution equations and the mathematical theory of the Schrödinger equation. His achievements are so great that we can safely claim that he was one of the founders of these theories and had set frameworks and standards for later generations. For instance, nowadays, it would be impossible for those who study mathematical fluid mechanics to be a specialist without reading his papers.

It was therefore a deep sorrow to hear of the news of his untimely death on October 2, 1999, which meant that his world of mathematics ended to advance all of sudden, and his papers of such perfect rigor and beauty would never appear. Then, some months later, we were told that Professor Heinz O. Cordes, Professor Kato's old friend, salvaged two of his unpublished manuscripts from an old personal computer in Professor Kato's study. On a kind permission by Mrs. Mizue Kato ( Professor Kato's wife ), these two manuscripts are included in the present volume of RIMS Kokyuroku. Although they are not complete in Professor Kato's standard ( he was a perfectionist ), they contain a new functional framework and interesting proofs of the existence of solutions of the Euler equations for incompressible inviscid fluid motion. We therefore came to the conclusion that they must be released to the scientific community in some form or other for future studies. The workshop was planned in order to make public these manuscripts left by Professor Kato as well as current works by those who remember and admire Professor Tosio Kato.

Though the workshop was carried out as a workshop of RIMS, Kyoto University, it would not be materialized without support from the Department of Mathematics of Hokkaido University. It is, in this regard, our pleasure to thank the department, in particular Professors Y. Giga and T. Ozawa, for the invitation to hold the workshop in Sapporo and their cooperation during the workshop. Support from Prof. Kenji Yajima should also be acknowledged. Invitation to some of foreign speakers were made possible by a kind aid from Inoue Foundation for Science.

Finally, on behalf of all the participants of the workshop and many Japanese mathematicians who appreciate Professor Kato's method and principle, let us thank Professor Cordes for his enthusiastic effort in salvaging Professor Kato's last manuscripts, in making them readable documents, and his coming all the way to Sapporo to give a lecture in memory of Professor Kato in Berkeley.

Editors Hiroshi Fujita S. T. Kuroda Hisashi Okamoto

## Tosio Kato's Method and Principle for Evolution Equations in Mathematical Physics

#### 京都大学数理解析研究所共同利用研究集会

研究代表者 岡本 久 (京大・数理研)

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日時: 2001年6月27日(水) 10:40 —

6月29日(金) 17:30

場所: 北海道大学 理学部 5 号館大講義室

#### Program

#### June 27th (Wed)

10:40-11:25 W. A. Strauss (Brown Univ.)

"Nonlinear instability of dispersive waves"

11:25-12:10 H. O. Cordes

"With Tosio Kato at Berkeley"

14:00-14:45 K. Ohkitani (Kyoto Univ.)

"Comparison between the Boussinesq and coupled Euler equations in two dimensions"

14:45-15:30 Y. Giga (Hokkaido Univ.)

"On the two-dimensional nonstationary vorticity equations"

16:00-16:45 K. Masuda (Meiji Univ.)

To be announced

16:45-17:30 H. Fujita (Tokai Univ.)

"Variational inequalities and nonlinear semi-groups applied to certain nonlinear problems for the Stokes equation"

#### June 28th (Thu)

10:40-11:25 J. T. Beale (Duke Univ.)

"Discretization of layer potentials and numerical Methods for water waves"

11:25-12:10 Y. Shibata (Waseda Univ.)

"On some stability theorem of Navier-Stokes equation in 3 dim. exterior domain"

14:00-14:45 H. Kozono (Tohoku Univ.)

"Asymptotic behaviour and net force for the Navier-Stokes flows in exterior domains"

14:45-15:30 Short Communications 1

H. Okamoto (Kyoto Univ.), K. Tanaka (Waseda Univ.)

K. Choe (Seoul National Univ.)

16:00-17:30 Short Communications 2

T. Abe (Waseda Univ.), M. Chae (Seoul National Univ.)

J. Kato (Hokkaido Univ.), O. Sawada (Hokkaido Univ.)

#### June 29th (Fri)

10:40-11:25 K. Yajima (Univ. Tokyo)

To be announced

11:25-12:10 S. T. Kuroda (Gakushuin Univ.)

"Resolvent formulas, special and general"

14:00–14:45 T. Ozawa (Hokkaido Univ.)

"Scatting problem for nonlinear Schrödinger and Hartree equations'

14:45–15:30 T. Ogawa (Kyushu Univ.)

"Analytic smoothing effect for the Benjamin-Ono equations"

16:00-16:45 D. Chae (Seoul National Univ.)

"Local existence and blow-up criterion of the Euler equations in the Besov and the Triebel-Lizorkin spaces"

16:45-17:30 M. Cannone (Université de Marne-la-Vallée)

"Asymptotic stability of solutions to the incompressible Navier-Stokes equations with external forces"

# Tosio Kato's Method and Principle for Evolution Equations in Mathematical Physics 研究集会報告集

### 2001年6月27日~6月29日 研究代表者 岡本 久(Hisashi Okamoto)

# 

	1.	With Tosio Kato at Berkeley	1
			H. O. Cordes
	2.	Discretization of Layer Potentials and Numeric	cal Methods for Water Waves18
		Duke Univ.	J. Thomas Beale
	3.	Incompressible Navier-Stokes equations in abs	stract Banach spaces27
		Univ. de Marne-la-Vallée	Marco Cannone
		Univ. Wrocławski	Grzegorz Karch
	4.	On the Well-Posedness of the Euler Equations	in the Besov and the Triebel-Lizorkin
		Spaces	42
		Seoul National Univ.	Dongho Chae
	5.	Asymptotic behaviour and net force for the Na	avier-Stokes flows in exterior domains58
		Yonsei Univ.	Hi Jun Choe
		東北大・理	小薗 英雄(Hideo Kozono)
	6.	Variational Inequalities and Nonlinear Semi-g	roups Applied to Certain Nonlinear
		Problems for the Stokes Equation	70
		東海大·教育開発研	藤田 宏(Hiroshi Fujita)
	7.	On the two-dimensional nonstationary vorticity	y equations86
		北大·理学	儀我 美一(Yoshikazu Giga)
	8.	Resolvent Formulas, Special and General	98
		学習院大·理	黒田 成俊(S. T. Kuroda)
	9.	Scattering problem for nonlinear Schrödinger	and Hartree equations105
		名大·多元数理	中西 賢次(Kenji Nakanishi)
		北大·理学	小澤 徹(Tohru Ozawa)
1	0.	ANALYTIC SMOOTHING EFFECT FOR T	HE BENJAMIN-ONO EQUATION113
		九大·数理	小川 卓克(Takayoshi Ogawa)
1	1.	Comparison between the Boussinesq and coup	
		dimensions	127
		京大·数理研	大木谷 耕司(Koji Ohkitani)
1	2.	ON A STABILITY THEOREM OF THE NA	
		IN A THREE DIMENSIONAL EXTERIOR	DOMAIN146
		早稲田大・理工	柴田 良弘(Yoshihiro Shibata)

13.	NONLINEAR INSTABILITY OF DISPERSIVE WAVES			
	Brown Univ.	Walter A. Strauss		
14.	Strichartz inequality and smoothing pro	operty for Schrödinger equations with potentia	l	
	superquadratic at infinity		179	
	東大·数理科学	谷島 賢二(Kenji Yajima)		
	· "	Guoping Zhang		
15.	On the Stokes and Navier-Stokes flows between parallel planes			
	早稲田大·理工	阿部 孝之(Takayuki Abe)		
16.	ON THE CAUCHY PROBLEM IN THE MAXWELL-CHERN-SIMONS-HIGGS			
	SYSTEM	***************************************	206	
	Seoul National Univ.	Dongho Chae		
	<i>II</i>	Myeongju Chae		
17.	On the Cauchy problem of the Chern-S	Simons-Higgs theory	213	
	Seoul National Univ.	Dongho Chae		
	n	Kwangseok Choe		
18.	Two-Dimensional Navier-Stokes Flow	with Nondecaying Initial Velocity	221	
	北大·理学	儀我 美一(Yoshikazu Giga)		
	道情報大	松井 伸也(Shin'ya Matsui)		
	北大·理学	沢田 宙広(Okihiro Sawada)		
19.	Weighted Strichartz estimates and exist	tence of self-similar solutions for semilinear		
	wave equations		228	
	北大·理学	加藤 淳(Jun Kato)		
	n	小澤 徹(Tohru Ozawa)		
20.	Blow-up problems modeled from the strain-vorticity dynamics			
	京大·数理研	大木谷 耕司(Koji Ohkitani)		
	IJ	岡本 久(Hisashi Okamoto)		
21.	ON THE STEADY FLOW OF COMP	RESSIBLE VISCOUS FLUID AND		
	ITS STABILITY WITH RESPECT TO	INITIAL DISTURBANCE	251	
	早稲田大・理工	田中 孝明(Koumei Tanaka)		
22.	Professor Tosio Kato		259	
23.	Two manuscripts left by late Professor	Tosio Kato in his personal computer	260	
	A remark on the 2 D-Euler equation	n	271	
	ere en	4		
24.	Publications of Tosio Kato	***************************************	275	
		and the second second second		
× ,	•			