# TO THE EXTENSION OF SOLUTIONS OF DIFFERENTIAL SYSTEMS Giuseppe Zampieri (Padova Univ.)

**ABSTRACT** We use the theory of microlocalization of sheaves of [K-S-2], and especially its formulation in [S] for boundary value problems to treat the extension of regular solutions of systems of P.D.E. across an 1-codimensional singular set. Let M be a real analytic manifold, X a complexification of M, N an analytic hypersurface of M,  $\Omega$  an open component of M  $\times$  N. For a suitable involutive manifold  $V \subset T_M^*X$ , invariant under the Hamiltonian flow of N x  $T_M^*X$ , we introduce a new complex  $B_{\Omega | X}^a$  of hyperfunctions in  $\Omega$  with real analytic parameters and study its applications to non-characteristic boundary value problems. In particular we show that the trace morphism preserves the analytic parameters. The analysis of  $\mathcal{B}^{\mathtt{a}}_{\Omega \, \mathsf{I} \, \mathsf{X}}$  could be performed from the viewpoint of the 2nd microlocalization at the boundary along V developped in [U-Z]; but we do not need to refer to such a general theory for the purpose of the present paper. We then consider a differential system M at x,  $x \in \mathbb{N}$ , and a closed set S, S  $\subset \mathbb{N}$ ,  $x \in \partial S$ . We denote by  $\forall$  the union of the leaves of  $V^{\mathbf{C}}$  issued from V, we let  $\rho$  be the projection  $Y \times T^*X \rightarrow T^*Y$ , and make the following hypotheses: the conormals to N at x are non-microcharacteristic for M along V in  $\pi^{-1}(x)$ ; char  $M \cap \rho^{-1} \rho(\{x\} \times V) \subset V$ ; i  $N_{X}^{*}(S) \subset V$  $\rho(\{x\} \times V)$ . We then prove that  $H^0(\mathcal{B}_{M|X}^a)$ -solutions of M on  $M \setminus S$  extend to Mat x. Under some additional assumptions on "propagation in the interior" we also obtain the extension of  $A_{
m M}$ -solutions. We refer to [Kan],  $[\hat{0}]$ , and [U-Z] for other results on continuation of (regular) solutions.

# § 1. THE COMPLEXES $B_{\Omega \mid X}^2$ AND $B_{\Omega \mid X}^a$

Let M = M'xL be real analytic manifolds with complexifications X = X'xZ and

dimensions  $n = n_1 + n_2$ . For a locally closed set A = A'xL of M, put A' = A'xZ and define (cf [K-S-2], [S])

$$(1.1) C_{A|X}^{h} = \mu_{\chi}(O_{\chi}) \otimes \omega_{M'/\chi'}[n_{1}] ,$$

$$(1.2) B_{A|X}^{2'} = R \Gamma_{T}^{*}_{X' \times L} (C_{A|X}^{h}) \otimes \omega_{L/Z}[n_{2}] .$$

We often consider the case A=M or A=N for an analytic submanifold  $N=N^{+}xL$  of M of codimension 1, or else  $A=\Omega$  where  $\Omega=\Omega^{\pm}$  are the components of  $M \cdot N$ . The following triangle will play an essential role:

$$(1.3) B_{N|X}^2 \rightarrow B_{M|X}^2 \rightarrow B_{\Omega}^2 + X \oplus B_{\Omega}^2 - X \rightarrow +1$$

**REMARK 1.1.** By the results of [U-Z] we could give a canonical definition of the complexes  $C_{*|X}^h$  and  $B_{*|X}^2$ , \*=M, N,  $\Omega$ , associated to a smooth conic regular involutive manifold V  $\subset T_M^n X$  such that

(1.4) V and N x 
$$T_{M}^{*}X$$
 intersect transversally,

and N  $\times$  V is regular involutive M

We recall from [K-L] that for \*=M, N,  $\mathcal{B}^2_{*|X}$  is concentrated in degree 0 and the natural morphism  $C_{\!\!\!|X|}|_{\mathsf{T}^*X'\times L}\to \mathcal{B}^2_{*|X}$  is injective,  $C_{*|X}$  being the sheaf of usual microfunctions. (As for the case  $*=\Omega$  it is proven in [U-Z] that  $(\mathcal{B}^2_{\Omega|X})_{\mathsf{T}^*_{\mathsf{M}^*}X'\times L}$  is concentrated in degree 0 but that the corresponding result on injectivity does not hold any more. However this is not needed here.)

We set now:

$$(1.5) B_{*|X}^{a} = R \Gamma_{M}(O_{X}|_{*xZ}) \otimes \omega_{L/Z} [n_{2}], * = M, N, \Omega.$$

For \* = M,  $\Omega$  we have a distinguished triangle

$$(1.6) B_{*|X}^{a} \rightarrow R \Gamma_{*}(B_{M}) \rightarrow R \pi_{*}(B_{*|X}^{2}) \rightarrow +1$$

( $\mathcal{B}_{\mathbf{M}}$  being the sheaf of hyperfunctions); for \*= N we have to shift

by -1 the first term of (1.6). Using (1.6), the results of [K-L], (and also the trick of the dummy variable for \* = N), one easily sees that  $\mathcal{B}^a_{*|X}$ , \* = M or N, are concentrated in degrees 0 and 1 with  $H^1(\mathcal{B}^a_{*|X}) \neq 0$ . The same should be proven for \* =  $\Omega$ ; but this is complicated and needless

here.

The detailed study of the complexes (1.5) is left to [U-Z]; we only treat here their applications to boundary value problems. Thus let  $\eta$  be a coherent  $\mathcal{D}_{\chi}$ -module on an open set of M. We assume all through this section that Y, the complexification of N, is non-characteristic for  $\eta$ .

## PROPOSITION 1.2. The natural morphisms

(1.7) 
$$H^0(\mathbf{R} \operatorname{Hom}(\mathbf{M}, C_{\Omega|X}))|_{\mathsf{T}^*X'xL} \rightarrow H^0(\mathbf{R} \operatorname{Hom}(\mathbf{M}, B_{\Omega|X}^2))$$
,

(1.8) 
$$H^0(\mathbf{R} \, \mathcal{H}^{\mathrm{om}}(\, \boldsymbol{\eta} \, , \, \mathcal{B}^{\mathrm{a}}_{\Omega \, | \, \chi} \, )) \rightarrow \mathcal{H}^{\mathrm{om}}(\, \boldsymbol{\eta} \, , \, \Gamma_{\Omega}(\, \mathcal{B}_{\mathrm{M}} \, ))$$
 are injective.

**PROOF.** By the results of [K-L] it is enough to prove (1.7) and (1.8) in  $T_{N}^{*}X'xL$  and N respectively. As for (1.7), set  $F = T_{M}^{*}X \oplus N^{*}(\Omega)^{a}$  ("a"= antipodal) and consider the commuting diagram

(1.9) 
$$c_{\Omega|X} \rightarrow B_{\Omega|X}^{2}$$

$$R \Gamma_{F} C_{N|X} [1] \rightarrow C_{N|X} [1] \rightarrow B_{N|X}^{2} [1] .$$

Then the conclusion follows from:

(1.10)  $\mu$ om(M,  $C_{N|X}$ ) = 0,  $\mu$ om(M,  $B_{N|X}^2$  /  $C_{N|X}$ ) $|T_{N}^*, X^* \times L$  = 0, which are in turn easy consequences of division formulas for  $C_{N|X}$  and  $B_{N|X}^2$  (cf [K-S-1]).

As for (1.8) we only need to recall (1.6) for  $*=\Omega$  , and use (1.3), and (1.10). The proof is complete.

Let  $m_{Y}$  denote the induced system by m on Y and let  $\gamma: \mathcal{H}om(m, \Gamma_{\Omega}(B_{M})) \rightarrow \mathcal{H}om(m_{Y}, B_{N})$  be the trace morphism (cf [S]). By collecting all above results we get:

### PROPOSITION 1.3. We have

$$(1.11) \qquad H^{0}(\mathbf{R} \operatorname{Hom}(\mathcal{M}, \mathcal{B}^{\mathbf{a}}_{\Omega \mid X}))_{X} = \{u \in \operatorname{Hom}(\mathcal{M}, \Gamma_{\Omega}(\mathcal{B}_{M}))\}_{X} :$$

$$SS(\gamma(u)) \cap (T_{N}^{*}, Y' \times L) \subset T_{Y}^{*}Y$$
,  $x \in M$ .

**PROOF.** Let  $\mathcal{F} = \mathbf{R} \ \mathcal{H}om(\mathcal{M}, \mathcal{O}_{\chi})$ , put  $\widetilde{\Omega} = \Omega' \times Z$ , and note that the natural diagram

$$(1.12) \qquad \pi^{-1} \ \mathsf{R} \ \Gamma_{\Omega} (\mathcal{F}) \qquad \rightarrow \qquad \mathsf{R} \ \Gamma_{\mathsf{T}}^{*} \chi^{\mathsf{T}} \times \mathsf{L}^{\mathsf{L}} \widetilde{\Omega} (\mathcal{F})$$

$$\downarrow^{\mathsf{L}} \mu_{\Omega} (\mathcal{F}) |_{\mathsf{T}}^{*} \chi^{\mathsf{T}} \times \mathsf{L}$$

is commuting. Thus recalling (1.6) and applying Proposition 1.2, we get

$$(1.13) \qquad H^{0}(\mathbf{R} \operatorname{Hom}(\mathcal{M}, \mathcal{B}_{\Omega \mid X}^{\mathbf{a}}))_{X} = \{ u \in \operatorname{Hom}(\mathcal{M}, \Gamma_{\Omega}(\mathcal{B}_{M}))_{X} : \\ SS_{\Omega}^{\mathcal{M}, 0}(u)_{\Omega}(\mathsf{T}^{*}X' \times \mathsf{L}) \subset \mathsf{T}_{X}^{*}X \}$$

where  $SS_{\Omega}^{M,0}(u)$  is the support of u identified to a section of  $H^0(\mathbf{R} \text{ Hom}(M, C_{\Omega X}))$  (cf [S]). According to [S] this is in turn equivalent to (1.11).

**REMARK 1.4.** When considering  $\mathcal{B}_{M|X}^{a}$  one can use the injectivity of  $C_{M|X}|_{T_{M}^{*}X'\times L}$   $\to \mathcal{B}_{M|X}^{2}$  and  $H^{0}(\mathcal{B}_{M|X}^{a}) \to \mathcal{B}_{M}$  as a substitute of Proposition 1.2. (Note that the latter injectivity follows from (1.6) and the (conical) flabbiness of  $\mathcal{B}_{M|X}^{2}$  (cf [K-L]).) Then using (1.12) one easily gets (1.14)  $H^{0}(\mathcal{B}_{M|X}^{a})_{x} = \{u \in (\mathcal{B}_{M})_{x} : SS(u) \cap (T_{M}^{*}X' \times L) \subset T_{x}^{*}X\}$ ,  $x \in M$ .

**REMARK 1.5.** For a regular involutive manifold V defined on the whole  $T_M^*X$  and satisfying (1.4), we can intrinsecally define  $\mathcal{B}_{*|X}^a$ , \*=M, N,  $\Omega$ , by replacing in (1.5)  $\overline{*} \times Z$  by  $\pi(\widehat{V}_{\overline{*}})$  (and  $\mathbf{w}_{L/Z}$  by  $\mathbf{w}_{V/\widehat{V}_{M}}$ ), where  $\widehat{V}_{\overline{*}}$  is the union of the leaves of  $V^{\mathbf{C}}$  issued from  $\overline{*} \times T_M^*X$ ; (we also write  $\widehat{V} = \widehat{V}_M$ ). One can also intrinsecally define the right hand sides of (1.11), (1.14) just by replacing  $T_{N}^*Y' \times L$  and  $T_{M}^*X' \times L$  by  $\rho \overline{\omega}^{-1}(V)$  and V respectively ( $\rho$  and  $\overline{\omega}$  being the natural mappings from  $Y \times T_M^*X$  to  $T_M^*Y$  and  $T_M^*X$  resp.).

It is then clear that if for some coordinates on M we can write

$$V = T_{M}^* X' \times L, \qquad N = N' \times L,$$

then (1.11) and (1.14) still hold. More generally owing to the invariance of  $B^2_{*|X}$  under contact transformation preserving V, N x V, and  $\omega_{N/M}$  (cf [U-Z]), one could prove that (1.6) is fulfilled. But this refined argument is not needed here.

#### § 2. EXTENSION OF SOLUTIONS WITH REAL ANALYTIC PARAMETERS

Let M be a real analytic manifold with complexification X, N an analytic hypersurface of M with complexification Y,  $\Omega = \Omega^{\pm}$  the two components of M \ N,  $\rho$  and  $\varpi$  the canonical mappings from Y x T X to T Y and T X respectively. X Let  $x \in M$ , let U  $\subset M$  be a neighborhood of x, and let V be a manifold in U x T X We assume that, in suitable coordinates on U:

(2.1) 
$$M = M' \times L$$
,  $X = X' \times Z$ ,  $N = N' \times L$   
 $V = T_{M'}^* X' \times L$ ,  $\hat{V} = T_{M'}^* X' \times Z$ .

Recall the complexes  $\mathcal{B}_{M \mid X}^{a}$ ,  $\mathcal{B}_{\Omega \mid X}^{a}$  (intrinsecally associated to V) and remember (1.11), (1.14). For any  $p \in \pi^{-1}(x)$  recall the identification  $T_{x}^{*}M \hookrightarrow T_{p}T^{*}X$  obtained through the embedding  $T^{*}X \times T^{*}X \hookrightarrow T^{*}T^{*}X$  and the Hamiltonian isomorphism, and observe that  $(T_{N}^{*}M)_{x}/R^{+}$  is just a pair of vectors  $\pm \theta$ .

THEOREM 2.1. Let N and V be defined, in suitable coordinates by (2.1), and let M be a coherent  $D_X$ -module at x which verifies

(2.2) 
$$\pm \theta \notin C_p(\text{ char } M, \hat{V}) = \frac{\text{for } \pm \theta \in (T_N^*M)_x/R^+}{\text{and for any } p \in \hat{\pi}^{-1}(x) \cap V,}$$

(2.3) 
$$\varpi^{-1}(\text{char } M) \cap \rho^{-1} \rho(\{x\} \times V) \subset T_{M}^{*} X$$

Let S be a closed subset of N with  $x \in \partial S$  and

(2.4) 
$$i N_{x}^{*}(S) \subset \rho \overline{\omega}^{-1}(V)_{x}$$
,

(in the identification i  $T^*N \simeq T_N^*Y$ ). We then have, in a neighborhood of x,

(2.5) 
$$\operatorname{Hom}(M, \Gamma_{M \setminus S}(H^0(\mathcal{B}^a_{M \mid X})) \stackrel{\sim}{\leftarrow} \operatorname{Hom}(M, H^0(\mathcal{B}^a_{M \mid X})).$$

**PROOF.** Let  $\Omega = \Omega^{\pm}$  with  $\Omega^{+} \cup \Omega^{-} = M \setminus N$ ; by reasoning as in § 1 and observing that

$$R_{\pi_*} R_{\Gamma_{(T_X^* X \cup_{\pi}^{\bullet}^{-1}(N))}(\mathcal{B}_{\Omega|X}^2)} = R_{\Gamma_{\Omega}}(\mathcal{B}_{M|X}^a),$$

we get a distinguished triangle

$$(2.6) \qquad \mathcal{B}_{\Omega|X}^{a} \rightarrow R \; \Gamma_{\Omega}(\mathcal{B}_{M|X}^{a}) \rightarrow R \; \mathring{\pi}_{*} \; R \; \Gamma_{\mathring{\pi}}^{\bullet} - 1_{(N)}(\mathcal{B}_{\Omega|X}^{2}) \qquad \stackrel{+1}{\rightarrow} \\ \text{Let } \mathcal{F} = R \; \text{Hom}(\mathcal{M}, C_{\Omega|X}^{h}) \Big|_{M \; \times \; T^{*}_{X}} \; \text{. We note that } (2.2) \; \text{implies } (p; \pm \theta) \not\in SS(\mathcal{F}) \\ \text{and thus also } R \; \Gamma_{\mathring{\pi}}^{\bullet} - 1_{(N)}(\mathcal{F}) = R \; \Gamma_{\mathring{\pi}}^{\bullet} - 1_{(M \times \Omega)}(\mathcal{F}) = 0. \; \text{By applying}$$

 $R \Gamma_{(N \times V \cap T_N^* X)}(.) [n_2]$  to the last equality  $(N \times V)$  being defined similarly to  $\hat{V}$  and  $n_2$  being the codimension of V), we then get, for a neighborhood U of x on N,

(2.7) 
$$R \Gamma_{\pi}^{\bullet-1}(N) R \operatorname{Hom}(M, B_{\Omega|X}^{2}) |_{U \times V} = 0.$$
Note now that (2.2) (2.3) imply:

Note now that (2.2), (2.3) imply:

$$\varpi^{-1}(\text{ char }M)\cap \rho^{-1}\rho(U\times V)\subset U\times V$$
 ,

which gives, combined with (2.7):

(2.8) 
$$R \pi_* R \Gamma_{\pi}^{-1}(N) R Hom(M, B_{\Omega|X}^2)|_{U} = 0.$$

By (2.6) this implies:

$$(2.9) \qquad \text{R } \mathcal{H}\text{om}(\ \textit{M}\ ,\ \mathcal{B}^{a}_{\Omega\,\big|\,X})\,\big|_{U} \ \simeq \ \text{R } \mathcal{H}\text{om}(\ \textit{M}\ ,\ \text{R } \Gamma_{\Omega}(\mathcal{B}^{a}_{M\,\big|\,X})\ )\,\big|_{U} \ .$$
 For  $u\in\mathcal{H}\text{om}(\ \textit{M},\Gamma_{M\smallsetminus S}(H^{0}(\mathcal{B}^{a}_{M\,\big|\,X})))$  let now  $u^{\pm}=u\big|_{\Omega^{\pm}}$ . Owing to (2.9) and (1.11) we get

$$SS(\gamma(u^{\pm})) \cap \rho(U \times V) \subset T_{\gamma}^{*}Y$$
.

We also clearly have

$$supp(\gamma(u^+) - \gamma(u^-)) \subset S.$$

Therefore the conclusion is an immediate consequence of the following two lemmas.

**LEMMA 2.2** (cf  $[\widehat{0}]$ ). Let F be a closed set of M and let  $u \in (B_M)_X$ ,  $x \in \partial F$ .

Then

$$SS(u) \cap N_{X}^{*}(F) \subset \{0\}$$

$$\{ supp(u) \subset F \qquad \Leftrightarrow u = 0 \}$$

PROOF. Easy application of Kashiwara-Holmgren's theorem and of sweeping out procedure by Bony-Schapira.

**LEMMA 2.3.** Let 
$$u \in Hom(M, \Gamma_{(M \setminus N)}(B_M))$$
; then

$$u \in \mathcal{H}om(M, H^0(\mathcal{B}_{N|X}^a)) \Leftrightarrow \{ \gamma(u^{\pm}) \in H^0(\mathcal{B}_{N|Y}^a) \\ \gamma(u^{\pm}) - \gamma(u^{-}) = 0. \}$$

PROOF. It is enough to recall the triangle

$$C_{\rm M|X} \rightarrow C_{\Omega}^+|_{\rm X} \oplus C_{\Omega}^-|_{\rm X} \rightarrow C_{\rm N|X}[1] \rightarrow {}^{+1}$$
 and the estimation

$$SS(u) \subset \bigcup_{\pm} SS_{\Omega^{\pm}}^{\uparrow \uparrow, 0} (u^{\pm}) \subset \rho^{-1} (\bigcup_{\pm} SS(\gamma(u^{\pm}))),$$
(cf [S]).

COROLLARY 2.4. In the situation of Theorem 2.1 assume in addition:

(2.10) 
$$\operatorname{Hom}(M, \Gamma_S(C_{M|X}))_p = 0 \quad \forall p \in T_M^* X \setminus V, \pi(p) = x.$$

Then (for  $A_M = O_X|_M$ ):

(2.11) 
$$Hom(M,\Gamma_{(M \setminus S)}(A_M))_{X} \simeq Hom(M,A_M)_{X}$$

By the argument in the proof of (2.7) and by the injectivity of  $C_{M|X|V} \rightarrow \mathcal{B}_{M|X}^2$ , a sufficient condition for (2.10) is that (2.2) is fulfilled for some  $V_p$  and  $\theta_p$  such that  $p \in V_p$ ,  $S \subset \{x \in M : \langle x, \theta_p \rangle \geq 0\}$ .

**REMARK 2.5.** It is clear from Lemma 2.2 that we can even consider in Theorem 2.1 some singular set S such that  $N_{x_0}^*(S) = T_{x_0}^*N$ . In fact for  $M = M'xL \simeq R^{n_1}xR^{n_2} \ni x = (x',x'')$ , we only need to assume that  $N \setminus S$  contains spheres of the L-plane whose diameters are infinite over the distance to  $\partial S$ . For example this is the case of any  $S \subset \{\phi \le 0\}$  for  $\phi \in C^0(N)$  with  $\phi(x_0) = 0$ ,

$$\partial x_{n_1} \Phi(x_0) \neq 0$$
,  $\partial_{x_1} \Phi(x_0) = 0$ ,  $\partial_{x_{n_1}} \Phi \in C^0$ ,  $\partial_{x_1} \Phi \in C^0$ .

**REMARK 2.6.** Theorem 2.1 extends the results of [Kan],  $[\hat{0}]$ . These are obtained by choosing  $L \simeq \mathbb{R}^{n-2} \subset \mathbb{M} \simeq \mathbb{R}^n$  and by replacing  $\hat{V}$  with  $T_M^* X$  in (2.2).

**EXAMPLE 2.7.** Let  $M = M'xL \ni (x',x'')$ , N = N'xL,  $M' = RxN' x' = (x_1,\overset{\sim}{x})$ , S = S'xL,  $x_0 = 0 \in \partial S$ . Let  $(z,\zeta)$ , z = x+iy,  $\zeta = \xi+i\eta$ , be coordinates in  $T^*X$ , let  $V = \{\eta'' = 0\}$  and consider

$$M : \zeta_1^2 - (z_1^r + \zeta^s)\zeta^2 + \zeta''^2$$
, r, s even,  $r \ge 2$ .

Then (2.2)-(2.4) hold with  $\pm\theta=\pm dx_1$  (cf [S-Z]) and thus we get (2.5) and (2.11) (as (2.10) is trivial in the present situation).

**EXAMPLE 2.8.** In the above situation let  $M' \simeq \mathbf{R} \times \mathbf{N}' \simeq \mathbf{R} \times \mathbf{R}^3$ , let  $V = \{\eta_3 = \eta_4 = \eta'' = 0\}$ , and consider  $M : (\zeta_1^3 + \zeta_3^3 + \zeta''^3, \zeta_2(\zeta_3^2 + \zeta_4^2))$ .

For S = S'xL with  $0 \in \partial S$  we have (2.2)-(2.4) and thus also (2.5). Moreover for any  $p \in V$  and for  $\pm \theta_p = \pm dx_1$  or  $\pm dx_2$  we have (2.2) with  $\hat{V}_p = T_M^*X$ . Therefore if we let  $S = \{x_1 = x_2 = 0\}$ , we get (2.10) and (2.11). (This extends Example 1.1 of  $[\hat{0}]$ .)

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