## 数理解析研究所講究録1249

# International Conference on Reaction-Diffusion Systems: Theory and Applications

京都大学数理解析研究所 2002年2月

#### Preface

Reaction-diffusion systems arise in continuous models for large number of physical, bioligical chedmical and other systems. Analytical and complementarily numerics of these systems have surprisingly revealed diversity of complex spatio-temporal patterns occurring in reacting-diffusing media. For instance, we can see that reaction-diffusion waves in chemical systems, nerve impilse propagation in neurophysiological systems, cell-differentiation and morphogenesis in biological systems and invasion of alien species in ecological systems have been intensively investigated.

As a special project research year held in April 2000–March 2001, Research Institute for Mathematical Sciences (RIMS) at Kyoto University, we organized an international conference on Reaction–Diffusion Systems: Theory and Applications, which was held in February 5–8, 2001.

This book contains a collection of the papers which survey recent developments of reaction-diffusion systems with theories and applications. The individual authors of this book were participants in this conference.

We would like to thank all of those who took part in the project reseach year, particularly the contributors in this conference. Also, we thank Grant-in-Aid for Scientific Research (A) 12304006, Grand-in-Aid for Scientific Research on Priority Area (B) 11214101 and Japan Association for Mathematical Sciences for

M. Mimura (Hiroshima University)

H. Okamoto (RIMS, Kyoto University)

support of this conference.

# International Conference

on

Reaction-Diffusion Systems: Theory and Applications

Organizers: Masayasu MIMURA and Hisashi OKAMOTO

Time: February 5(Monday) ~February 8(Thursday), 2001

Place: Room 420, RIMS, Kyoto University

February 5 (M 13:00-13:10		Masayasu Mimura (Hiroshima University)	
13:10-13:50 Rec	• •	versity of Minnesota, U.S.A.) Lotka-Volterra competition system with cross-c	liffusion
14:00-14:40	<b>Eiji Yanagida</b> (To Stability a	ohoku University) nalysis for shadow systems	and the second
14:50-15:20	break	j bjil storfille elleretane e ellereta	
		(University of Paris-Sud, France) action-diffusion system with resource-consume	er interaction
16:10-16:50		(Ryukoku University) spects of vortices in the Ginzburg-Landau equa	ntion
February 6 (1 10:00-10:40	Takashi Suzuki (	Osaka University) ons for a parabolic elliptic system modelling che	emotaxis
10:50-11:30		(Taiwan Normal University, Taiwan) behaviour for a quasi-linear parabolic equation	erij Berij Bliss
11:40-12:20		<b>moto</b> (Hiroshima University) nsition layers intersecting the boundary of dom jusion systems	ain
12:30-14:00	Lunch break		
14:00-14:40		Utrecht University, Netherlands) silinear population models	
14:50-15:20	break		
15:20-16:00	Yasumasa Nishi	<b>ura</b> (Hokkaido University)	

16:10--16:50 Miguel Herrero (Complutense University of Madrid, Spain)

Geometrical approach to complex dynamics in dissipative systems

Lines and nets:models of filamentary structures

February 7 (	Wednesday)
10:00-10:40	Marianito Rodrigo (Hiroshima University)  Exact solutions and front dynamics of reaction-diffusion systems
	Hiroshi Matano (University of Tokyo)  Travelling waves in spatially inhomogeneous media the non-periodic case
11:40-12:20	Michel Chipot (University of Zurich, Switzerland) On the asymptotic behaviour of the solution of parabolic problems in cylindrical domains becoming unbounded
12:20-14:00	Lunch break
14:00-14:40	Paul Fife (University of Utah, U.S.A.)  The intricacies of grain boundary movement
14:50-15:20	break
15:20-16:00	Shin-Ichiro El (Yokohama City University)  Dynamics of pulse-like localized solutions in reaction-diffusion systems
16:10-16:50	Alberto Tesel (University of Roma, Italy) On a class of parabolic equations with variable density and absorption
February 8 (	Thursday)
10:00-10:40	• *
10:50-11:30 <i>Ph</i>	Nobuyuki Kenmochi (Chiba University) ase change problems arising in the Czochralski Process of Crystal Growth
11:40-12:20 Red	Jose Francisco Rodrigues (University of Lisbon, Portugal) action-diffusion: from systems to nonlocal equations
12.30 Clos	ing address

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